

# Recursive Equation Approach of Information Hiding for Authentication of Digital Data

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## ABSTRACT

As the Information communication technology advances, it has become crucial to ensure the originality of digital content. This paper focuses on using recursive equation approach of steganography to ensure authenticity of digital content. This is achieved by embedding hash value of the digital data in the same digital file. In this paper, we have taken 24 bit BMP files to implement the concept. We have used recursive equation of any order as key to find pixel location in the BMP file to embed the 128 bit MD5 value of the BMP file before its transmission. At the receiving end the MD5 is extracted from the zero bytes of BMP file and the original bits in extra bytes are restored before computing the MD5 value of the received and restored BMP. The two MD5 values are compared. Equality of the value authenticates the originality of BMP file.

**Keywords-** steganography, recursive equation, MD5, hash value, authenticity.

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## 1. INTRODUCTION

With the commencement of computer and its ever expanding application in different areas of life, the concern of information security has become gradually important. Different methods have been adopted to provide security to digital content such as cryptography and steganography etc. Besides implementing steganographic approach, it has also become important to ensure the authenticity of digital content. No unauthorized user should be able to hamper originality of digital content[18]. For secure communication, not only security of information is important but also source from where the information is originated is also required [1]. With confidentiality, authentication of original message is also essential. Different methods have been used to verify the originality of the digital information. This paper proposes to use recursive equation method of steganography to hide MD5 Hash in 24 bit BMP file format[13] and then verifying the authenticity of BMP file after obtaining the hash value using MD5 algorithm.

### 1.1 Steganography

Information hiding is the process of hiding the information in any media e.g text, images audio etc. Steganography means covered writing [2].Steganography is used for hiding information in digital format to fleece the existence of hidden information [3]. Steganography is an art used to maintain confidentiality of information [4]. The purpose of steganography is to hide the fact that communication is taking place. For establishing steganographic communication, an embedding and extraction algorithm with optionally a key is needed[5]. Steganography may be classified as pure, Symmetric and asymmetric steganography[18]. In pure steganography, no secret key is shared between sender and receiver whereas in symmetric and asymmetric steganography, a key is shared between two parties [6].In the proposed system pure steganography is used. Most important factor in steganography is the type of medium used in steganography .Highly recommended medium for steganography is image because we may get different randomized pixel locations in image file to hide information. Images can be used as potential medium for hiding information because of its attractiveness. Because of this advantage, In this paper we are using 24 bit BMP file as a medium to verify the originality of digital content by hiding MD5 hash value in 24-bit bmp file[16].

### 1.2 Bitmap Format

Bmp files are simple and large in size and due to this advantage, these files have got wide acceptance in windows programs. The Microsoft Windows bitmap file format can support a lot of different options, including compression, different bit depths, etc [7].Bitmap files can be stored in different bit depths which determines number of bits used in color palette for each pixel. One bit bmp file format use only one colour, 4 bit bmp uses 16 colours, 8 bit uses 256 colours and 24 bit bmp uses

$2^{24}$  bit colour combinations for each pixel[20]. We are using BMP file format to explain our approach.

The bitmap file formats can use little endian or big endian format to store values in file. In little endian format, the low-order byte of the number is stored in memory at the lowest address, and the high-order byte at the highest address. For example, a 4 byte Long integer will be written as

Byte3 Byte2 Byte1 Byte0

Whereas in Big endian format, the high-order byte of the number is stored in memory at the lowest address, and the low-order byte at the highest address. For example, a 4 byte long integer would be written as:

Byte0 Byte1 Byte2 Byte3

The .bmp file format requires that the digital content in a scan line (horizontal line) in the image should be aligned on a 4-byte boundary, so every line must end with 4 byte boundary. This means that width of an image must be a multiple of 4. If the width of bmp image file is not in multiple of 4 then extra bytes are padded. These Extra bytes are also termed as zero bytes.

In 24 bit bmp, 3 bytes are used to represent a single pixel. So to align a 24 bit bmp along a scan line, (width \*3) must be a multiple of 4. For e.g. If we consider a 24 bit bmp image of size 70\*80. The total size of bmp file is 5600 pixels which has 70 columns(width) and 80 rows(height). In a single scan line,  $70 * 3 = 210$  bytes need to be stored but as 210 is not a multiple of 4, padding is required. For Padding, we require extra bytes and it can be calculated by the following formula:

$$\text{Extra bytes} = (4 - (3 * \text{width}) \% 4) \% 4$$

In the above example for storing 210 bytes, 2 extra bytes are required. So in each single line, 212 bytes are required, which includes 210 actual data along with 2 extra or zero bytes. This paper proposes to use 24 bit bmp and a recursive equation approach for hiding message digest to verify the authenticity of the source of file by using extra bytes of bmp file.

### 1.3 Message Digest

Message digest is a type of cryptographic hash value which can be used to ensure integrity and authenticity of a message. In the context of message verification, a hash function takes input message of any length and delivers a fixed size output. The output is referred as hash or the message digest. The message digest depends totally on bits in input message. The benefit of creating message digest is that a minor change in the input message can totally change its message digest. If during transmission an intruder tries to make any alteration in input message then its message digest would also be changes and will not match the original message digest. To obtain message digest different algorithms like MD5 and SHA-1[8] are used[14, 15]. The obtained message digest from hash function varies in length from 128 bits to 160 bits depending upon the algorithm used [9]. Practically all algorithms divide the long message into equal size blocks and then message is processed block by block in an iterative manner to generate its digest.

## 2. Recursive Equation approach

A sequence is an enumerated collection of objects. Sequence can be explicit or recursive. A **recursive definition** consists of two parts. First is recurrence relation and second is an initial condition[17]. Recurrence relation is an equation that uses a formula to generate next term in the sequence based on previous term and to generate first term, initial condition is required[10]. Recursive equation always have initial condition to get first term and then it repeats itself to generate next terms[21]. In computer science, Recursive methods are used to repeat itself to generate the output[11]. In the proposed paper, we are using recursive equation to generate recursive pixel positions to hide MD5 hash code in .bmp file format to verify the originality of digital content

## 3. Conceptual Approach

Although MD5 hash codes are difficult to crack for an intruder, to provide one more layer of security we are using recursive approach to hide message digest in cover file[12]. This paper focuses on using 24 bit bmp file to hide hash code to verify the originality of the source file. The MD5 hash code is hidden using recursive equation approach. The recursive equation produces different randomized locations in .bmp file to hide hash code in extra bytes of bmp file[11]. As this paper proposes to hide the message digest in extra bytes, the quality of bmp image will not be degraded. To hide message digest, we are only using the extra bytes which are used to pad the image to provide 4 byte boundary. The concept of paper is based on message digest, recursive equation and 24 bit bmp file.

The concept is explained in below mentioned steps:

- 3.1 The 128 bit message digest generated by MD5 algorithm will be hidden in 24 bit bmp file.
- 3.2 To hide this message digest, extra bytes of bmp file are used. Initially all 16 bits in extra byte will be initialized with number 0 to signify that bit places are vacant and can be used to store message digest
- 3.3 Recursive equation generates the bit position to find the location in bmp file.. The generated bit position is then moved to first bit of 2 extra bytes at the end of each scan line
- 3.4 Different bit locations will be generated by recursive equation. First 2 bit positions generated by recursive equation will be used for hiding 2 bits of message digest. The generated bit positions by recursive equation will be moved to first 2 bit position in extra bytes.
- 3.5 The algorithm will check for free space in 2 extra bytes i.e. 16 bits. If first 2 bits of extra byte have 0 values then 2 bits from 128 bit message digest will be stored in first 2 bits of extra byte and then for storing next 2 bits of message digest, we will check if the next 2 bits from remaining 14 bits of extra byte have 0 value then at these locations we will hide next 2 bits from remaining 126 bits of message digest and this way we will hide 128 bits of message digest in extra bytes
- 3.6 Masking is used to hide bits from message digest in extra bytes

Figure 1 shows the process of checking authenticity of digital content

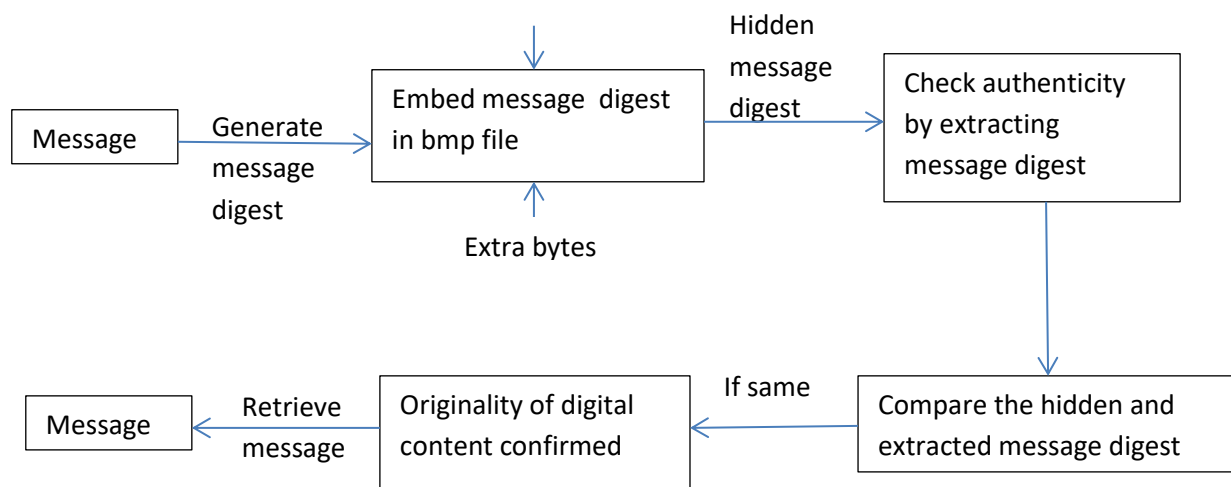


Figure 1

#### 4. IMPLEMENTATION

4.1 Consider a hexadecimal message digest as d50ea9e8881e8b2d e2dd75074a230533 to be hidden in 24 bit bmp file. The generated message digest of 128 bits will be hidden in extra bytes of bmp file. 2 bits from 128 bit message digest will be stored in extra bytes in each scan line. So we need minimum 64 positions to hide 128 bit message digest.

4.2 Let the size of bmp file is 70\*80. As each scan line requires a multiple of 4, the width of the image need to be padded accordingly. So to store 210 bytes in each scan line, we need 2 extra bytes to make it 212 bytes which is a multiple of 4. The generated message digest will be stored in these 2 extra bytes in each line.

4.3 Total size of image = 70 \* 80 \* 3 = 16800 bytes but as we know in each single line the padding is added. In our example we have considered padding of 2 bytes to make it a multiple of 4 in single row.

So total size after padding in all 80 rows =  $16800 + (2 \times 80)$   
 $= 16800 + 160$   
 $= 16960$  bytes

Following table explains the process of hiding message digest in nearest zero byte.

Table 1

Actual Data Bytes		Zero Bytes															
1	16 53 175	210															212
213		422															424
425	578	634															636
637		846															848
849		1058															1060
1061		1270															1272
1273		1482															1484
1485		1694															1696
1697		1906															1908
1909	1909	2118															2120
2121		2330															2332
2333		2542															2544
2545		2754															2756
2757		2966															2968
2969		3178															3180
3181		3390															3392
3393		3602															3604
3605		3814															3816
3817	3864	4026															4028
4029		4238															4240
4241		4450															4452
4453		4662															4664
4665		4874															4876
4877		5086															5088
5089		5298															5300
5301		5510															5512
5513		5722															5724
5723		5934															5936

4.4

Using recursive equation, generate the pixel locations to hide message digest

Let the equation be

$$t_n = at_{n-1} + t_{n-2}$$

Constant value of  $a=7$

Initial value of  $t_0=1$

Initial value of  $t_1=5$

Also take a single dimensional array, let  $a$  be an array. The array will hold the locations generated by a recursive equation. Initially all places in array will have zero value which implies free space is available. The purpose of using array is to store the locations of hidden message digest

$$S_0, t_2 = 3 \times t_1 + t_0 \\ = 3 \times 5 + 1 = 16$$

First place generated by recursive equation is 16 so 2 bits from message digest will be stored in nearest zero byte. In this case as 16<sup>th</sup> byte position is nearest to zero byte in first scan line so 2 bits from message digest will be stored in 211<sup>th</sup> byte location starting from LSB bit of 211<sup>th</sup> byte.

we have considered message digest in hexadecimal form

message digest = d50ea9e8881e8b2d e2dd75074a230533

The first two bits to be hidden are 11 which is taken from the hexadecimal value of d whose binary equivalent is 1101. Lets consider a character CH=00000000 (all clear bits of 211<sup>th</sup> byte)

CH1=00000001 (first bit to be hidden in 211<sup>th</sup> byte)

We will perform OR operation between CH and CH1

CH || CH1 which is also called masking.

CH= 00000000

CH1=00000001

OR 00000001

So after performing OR operation, 211<sup>th</sup> byte will have 00000001 bits. Now to hide another bit i.e. 1 again, perform OR operation again. Consider ORing output as new 211<sup>th</sup> byte so new ch = 00000001 and to hide another bit 1 in 211<sup>th</sup> byte, new ch1=00000010 is considered.

CH = 00000001

CH1= 00000010

OR 00000011

By following above procedure, we have successfully hidden 2 bits from 1101 which is equivalent of 'd' in 211<sup>th</sup> extra byte. Now to hide next 2 bits i.e. 01, next location need to be generated using recursive equation.

$$t_3 = 3 * t_2 + t_1 = 3 * 16 + 5 = 53$$

From remaining 126 bits of message digest, next 2 bits i.e. 01 will be hidden in the extra byte nearest to 53<sup>rd</sup> location generated by recursive equation. So nearest extra byte is again 211<sup>th</sup> byte. As we have already hidden 2 bits in 211<sup>th</sup> byte and resultant 211<sup>th</sup> byte after hiding first 2 bits is 00000011.

To hide third bit i.e. 0, nothing need to be done as in 211<sup>th</sup> byte, it is already 0 at third LSB location so no need to make any change in current 211<sup>th</sup> byte. To hide fourth bit i.e., 1, again we have to perform OR operation.

CH =00000011 (211<sup>th</sup> byte)

CH1=00001000 (Bit presentation to hide 1 at fourth bit position)

OR 00001011

The 211<sup>th</sup> byte after hiding four bits looks like 00001011. The first 4 bits which are represented as 'd' in message digest is completely hidden. To hide next 2 bits from remaining 124 bits message digest, binary equivalent of 5 is considered which is 0101. So now 01 will be hidden at new bit position generated by recursive equation.

$$t_4 = 3 * t_3 + t_2 = 3 * 53 + 16 = 175$$

The equation generated 175<sup>th</sup> location which is again near to 211<sup>th</sup> byte. As already 4 bits of 211<sup>th</sup> byte have been used to hide 4 bits of message digest, next 2 bits i.e. 01 from message digest will be hidden at 5<sup>th</sup> and 6<sup>th</sup> bit position of 211<sup>th</sup> byte. To hide '0', no need to make any change in current 211<sup>th</sup> byte as 0 is already stored at 5<sup>th</sup> bit position of 211<sup>th</sup> byte. Next bit to be hidden is 1 at 6<sup>th</sup> bit position of 211<sup>th</sup> byte. Again we will perform masking to hide the bit.

CH = 00001011 (211<sup>th</sup> byte)

CH1= 00100000 (Bit presentation to hide 1 at sixth bit position)

OR = 00101011

The 211<sup>th</sup> byte after hiding six bits looks like 00101011. Till now we have hidden 6 bits from message digest. New bit position needs to be generated to hide next 2 bits i.e., 01

Next location generated by recursive equation is :

$$t_5 = 3 * t_4 + t_3 = 3 * 175 + 53 = 578$$

t<sub>5</sub> has generated 578<sup>th</sup> byte location and its nearest extra byte is 635. Now next 2 bits i.e., 01 will be hidden in 635<sup>th</sup> extra byte. Initially all bits of 635<sup>th</sup> byte will be clear i.e., 00000000. To hide '0' which is seventh bit of message digest, no change is needed because '0' is already stored there. To hide seventh bit, 635<sup>th</sup> byte need to be changed by performing OR operation with new mask bits.

CH = 00000000 (635<sup>th</sup> byte)

CH1 = 00000010 (masking bits to hide 1 at second LSB position of 635<sup>th</sup> byte location)

OR      00000010

So 2 least significant bits from 635<sup>th</sup> byte are occupied as we have hidden seventh and eighth bit from message digest. Now from message digest d50ea9e8881e8b2d e2dd75074a230533, we have already hidden 8 bits which means d5 is completely hidden. To hide next bits, consider hexadecimal 0 whose binary equivalent is 0000. From right side, we will hide 2 bits at next location.

The next location generated by equation is as follows:

$$t_6 = 3 * t_5 + t_4 = 3 * 578 + 175 = 1909$$

The equation generated 1909<sup>th</sup> byte location which is near to 2119<sup>th</sup> zero byte. So next 2 bits from message digest i.e., 00 will be hidden in 2 least significant bits of 2119<sup>th</sup> byte. As per the algorithm, no masking bits are needed as 2 least significant bits are already having 0 value.

The same process is followed to hide complete 128 bit message digest in zero bytes.

## 5 CONCLUSIONS

The algorithm that has been proposed provides a solution to hide message digest in extra bytes of BMP file format. Hiding secret data in extra bytes has one very crucial advantage of not hampering the quality of image at all. Because the data is concealed in 24 bit BMP, it does not harm the quality of image. As the proposed algorithm hides the data only in extra bytes of image, the intruder will not be able to even detect the presence of hidden data because the actual bits are not disturbed at all to hide data.

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