

A Comprehensive Study on Design and Development of Optical Image Encryption Techniques

Anshika Malsaria,

Manipal University Jaipur

Pankaj Vyas,

Associate Professor, Manipal University Jaipur

Manjit Kaur,

Gwangju Institute of Science and Technology

ABSTRACT

Since image processing algorithms can work with a vast volume of data easily, optical cryptographic techniques are commonly used in image security. Since the proposed DRPE, image encryption in particular has gotten a lot of coverage. DRPE employs various approaches for example-4f and Fourier Transform (FT) to encrypt local as well as spectral data; image encryption is done on the basis of input along with the Fourier planes using random phase coding. The complete process of encryption transforms the input image to a white sound in this manner. Confidentiality is obtained by the method of translation. Only when the information of location and the secret key are perfectly matched would the secret picture be revealed. Random category masks may be thought of as hidden keys in general, and since the key space is too big, blind deconvolution alone is insufficient to reconstruct the original picture. The standard DRPE methodology was discussed in this paper, as well as its numerical emulation, sampling considerations in the spatial as well as frequency domains, and the benefits and drawbacks of different transforms. Additionally, certain optical coding and scrambling methods are investigated. The paper ends with a discussion of recent advances in the area of optical image encryption, as well as a look forward to the future challenges.

Keywords: DRPE, AES, Ptychography, Cryptography, Re-Encryption

Introduction

The popularity of the internet is growing day by day. Information like text, images, videos are widely transferred over the Internet. All the Information are prevented with some mean of security parameters that provide legitimate user authentication. A variety of encryption algorithms are present to secure communication channels. The majority of internet users do not aware of the security implemented on channels. As the digital market is growing, the security issues are also growing. In many online transactions, the user's identity is very important. Securing the authentication details based on various security mechanisms requires. Without protection personal and companies' information may be at high risk. A lot of money spent on research and development of security algorithm and technologies. Military services also require a highly secure platform to transfer secret information over secure lines. Most of the information is image-based. So, the requirement of a good security mechanism otherwise the important information will be open for security threats like modification, duplication, eavesdropping [1-10]. Optical encryption technology comes into light after the proposal of Réfrégier and Javidi (1995) Double random phase encryption. Optical encryption has the capability of high speed and parallel processing. Double random phase encryption works in various domains like fraction Fourier transform, Fresnel transform, Linear canonical transform, Gyrator transform, Hartley transform. These transforms help the DRPE to improve flexibility, security, and implementation. The main advantages of optical encryption are - (i) Optical instruments having capabilities of parallel processing (modulator and lenses). (ii) Optical encryption method having capabilities to work in multidimensional and multiple parameters. (iii) optical encryption requires the knowledge of optics, computer

applications, image processing, signal processing so attackers need to understand all the things before attacking the optics cryptosystem [81-85].

Most image encryption researches in past years based on the DRPE encryption technique. It's built on the 4f optical system idea. In image processing, random-phase encoding is used to encode the input and Fourier planes. Since, DRPE (acronym for double random phase encryption) performs various image multiplication with the help of random phase mask (RPM) in both the spatial and temporal domains (DRPE). The input picture is transformed to white noise during the encryption process. The encrypted image is captured using digital holographic technologies. In the encryption method, the second RPM serves as a

hidden key. The method of decryption is the opposite of encryption. The original picture will reform if the hidden key and its spatial details are perfectly balanced. Two concerns with DRPE were found. The hidden keys, for instance, are the same resolution as the original pic, which is way too high. Second, since DFT-DRPE needs a lot of room, the computational cost is very high.

The architecture of the (DRPE) method is used to study the optical encryption technique in this article [11-30]. The optical surveillance system's benefits and drawbacks are discussed. This analysis would provide useful information about existing optical protection system technologies which will aid in future innovations. There are three purposes of this article.:

- (i) The project was based on a detailed review of current optical image encryption techniques.
- (ii) Considering all possible cryptanalysis methods.
- (iii) There are benefits and disadvantages to of optical image encryption technique. Some methods are resistant to a number of threats, but they have problems with computational speed and latency. As a result, the difference between computational speed and efficiency against different security threats must be explored.

This paper's major contributions are as follows::

A thorough investigation of various optical image encryption methods was carried out. The various transforms, as well as traditional DRPE and efficiency tests, have been explored in relation to optical image encryption techniques. Differential and key tests have been conducted on current encryption methods. Future research directions in the development of effective optical image encryption techniques have been investigated.

1. Structural analysis of DRPE technique

The implementation of DRPE is done by making the optical setup called 4f is shown in Figure 1. [4]

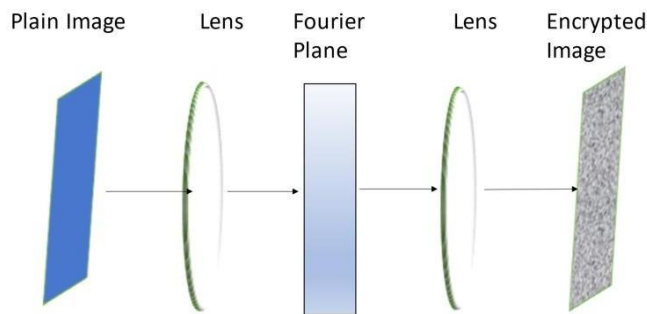


Figure 1: DRPE 4f setup

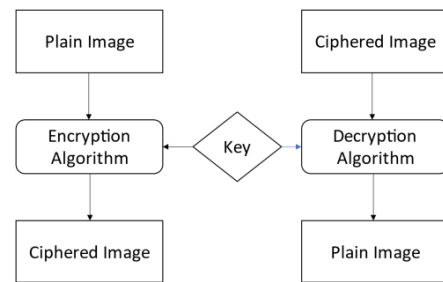


Figure 2: General approach for image encryption

Here a filter performs the masking and then the second activity will done by lens that is the inverse Fourier transform⁻¹ in the output plane to get the encrypted image. There are only two-phase plates in DRPE which are used as a secret key. To improve performance and key, fractional Fourier transform (FRT) was used with the DRPE scheme [8]. There are three planes in DRPE: input plane, second is encrypted plane, and third is output plane. The keyspace is larger than traditional DRPE as the FRT is having three parameters that connect any two out of three planes; so, the secret key is two-phase plates. FRT based DRPE also having six parameters which used as the secret keys.

Working of DRPE (Double Random Phase Encryption)

In this part, DPPE is discussed along with its encryption and decryption techniques.

Encryption-

Always encryption of image based on hiding the image which is then generated by the cipher image using some algorithm with keys. In Figure 2 DRPE encryption method is shown. Here in the DRPE technique first the image monochromatic waves pass from propagator 1 (P1) having plane (x, y) then the OFT (optical Fourier transform) takes place on P1, then Propagator 2 P2 having plane (x, y), then again OFT2 of the plain image and finally the cipher image is obtained. All the terms come in Fourier optics image processing techniques. Alike quantum optics, optical sources information needs to be extracted by the mean of some informative tool [8]. The spatial frequency domain (kx, ky) as the conjugate of the spatial (x, y) domain is

used in Fourier optics. The two propagators in DRPE encoding $P1(x, y)$ and $P2(x, y)$ are independent phase function and worked in spatial and frequency domain.

Refrégier and Javidi [5] proposed the DRPE technique. This technique is based on the 4f setup (Fig. 1) that, along with the spectrum, transforms the image as input into white noise. Since images have RGB density, converting RGB to white density is needed to encrypt input images. To encrypt an image, a switch in both amplification and position knowledge is available. because at the decryption process with amplitude or phase spectral information the plain image can be reformed. Cipher image is complex value so to obtain amplitude and phase information is necessary.

$$E(x, y) = DRPE(I(x, y), P1(x, y), P2(x, y)) = OFT(I(x, y) \times P1(x, y) \times P2(x, y))$$

(1)

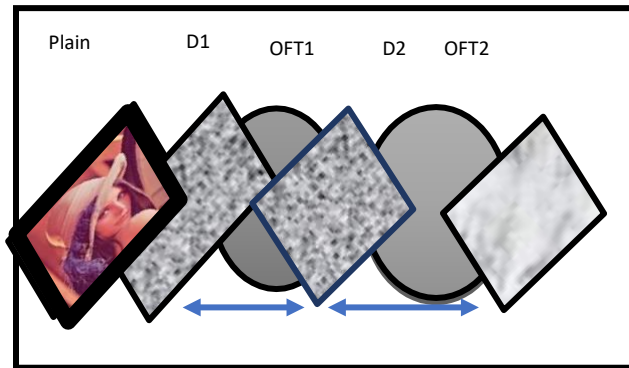


Figure 3. Encryption in DRPE

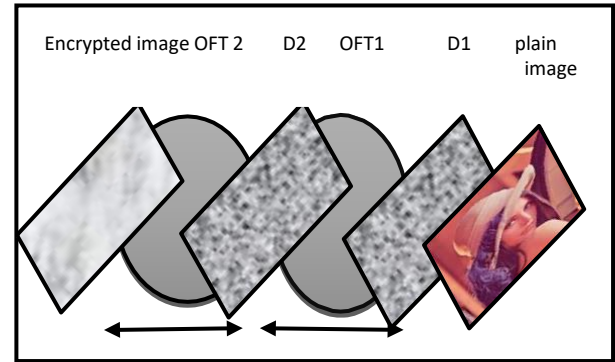


Figure 4. Decryption in DRPE

Decryption-

For decryption (ref Figure 4) the inverse process of DRPE is performed using two diffusers just like encryption and calculate their inverse optical Fourier transform.

$$\begin{aligned} (x, y) &= DRPE^{-1}(E(x, y), P1(x, y), P2(x, y)) \\ &= DRPE(E(x, y), P1 \times (-x, -y), P2 \times (-x, -y)) \end{aligned} \quad (2)$$

2. Literature Survey

A literature survey contains a review of various existing optical image encryption techniques transforms. This section discusses various DRPE transformations that are used in optical encryption algorithms to convert images in the spatial and frequency domain. They all contribute to the security of an algorithm for optical image encryption.

The joint transform correlator (JTC) [2] is used to propose optical image encryption. The initial picture and one of the stage plates are inserted into the JCT input plane in this work as encryption keys. After that, the Fourier Transform is used. The Fourier combined spectrum of combined energy is available as an enclosed image after conversion. A step pad, which serves as a reduction key, is placed in the appropriate location on the space shuttle during the deceleration period. By filtering the background frequency and converting the Fourier variables, the encrypted image is programmed on the Fourier spectrum plane. JTC encryption thus overcomes the limitations of standard DRPE. The encrypted image is accessible and does not require the use of a complex stage plate as a hidden key since it is based on Fourier's power output. The consistency of the dissipation is unchanged by improving the secret key in the input plane because it just improves the form of the hidden image.

In 2004, a new approach for embedding images on the Fresnel domain [6] was suggested. It has three planes: one for input, one for encryption, and one for output. Unlike other encryption techniques, this one does not need lenses; instead, it encrypts images using the Fresnel look. The first picture is pre-edited using a phase plate on the input plane during the encryption process. The picture is then continued in the encryption plane and modeled a second time using the Fresnel axis. Finally, the Fresnel distribution is used at the same time. Not only are the two type plates used as hidden keys in the encryption process, but the two levels of use are also used as keys.

The most commonly used encryption algorithm today is chaos-based encryption. The conflict method [9] is a strong non-linear system capable of generating a random sequence of good and suitable data encryption. To encrypt the records, a

turbulent scheme was proposed [10]. Since then, chaotic cryptography has gotten a lot of coverage as a branch of cryptography. Digital images are then encrypted with the help of a chaotic mapping approach for example- the CKBA encryption method, Kolmogorov-based encryption schemes, picture transformations and encryption, and random map-based encryption, which is generated by a complex system.

In paper [11] proposes another approach based on encryption which is the sensation of compression and double- phase randomization, which can complete image compression while still providing simultaneous encryption. To construct a measuring matrix with two random phase covers, we use a hyperchaotic method. The first image is then calculated using a matrix scale to achieve simultaneous encryption and compression, in which the compressed image is rewritten by encoding a random process with two random phase masks, and eventually the resulting image is confused and separated using a hyperchaotic method.

The Differential Evolution (DE) approach is used in this paper [12] to implement a new effective techniques for the encryption of image encryption based on the magnitude and deception of a section. The delivery of the keyed discrete Fourier transform (DFT) it operate on the principle of DE for the encryption purposes is the work's breakthrough. The hidden key has been exchanged between encryption and decryption until now. On the first image to be nailed, a four-dimensional (2-D) transformation is performed first. Second, using the Linear Feedback Shift Register (LFSR) generator, a crossover was performed between two sections of the encrypted picture. Similarly, based on the LFSR reference generator, main changes are made to the individual components of such chosen objects. To ensure the protection of emerging indices, the LFSR index creator starts the seed with a shared secret key. The picture pixels' locations are altered as a result of the operation. A new image encryption scheme based on the DE system and constructed with a simple delivery method is being created. The descriptive technique is a structured procedure that employs the same key. This embedded picture is found to be entirely skewed, allowing the planned work to become more rigid. The suggested image encryption scheme is verified by imitation results.

With the exponential growth of electronic data sharing, data protection for data collection and dissemination has become increasingly necessary. Since photographs are widely used in manufacturing processes, it is critical to safeguard sensitive image data against unauthorized entry. We evaluated existing image encryption methods and compression added two of them in this paper [13]. (Screen encryption such as Mirror and Visual Cryptography). The proposed approaches have been implemented for the sake of research. The study' findings are presented in this article.

Digital Signatures and Graphics Encryption Technology: A new approach for encrypting safe image transfer has been suggested by Aloka Sinha and Kehar Singh [19]. The original edition of the original photograph has an optical digital signature attached to it. The required debugging code, such as Bose Chaudhuri Hochquenghem (BCH)code, is used to encode the images. Since the image has been removed from the recipient, a digital signature may be used to check the image's validity.

Lost Image Encoding and Encryption Using Scanner: SS Maniccam and N.G. Bourbakis [20] have developed a modern approach for compressing and encrypting binary and gray pictures that is unmistakable. The SCAN approach produces SCAN patterns, which are used in focus and encryption schemes. SCAN is a two-dimensional, two-pronged method for locating a good location.

Fractional Fourier Transform (FFT)

The Fourier transform (FT) is further subdivided into Fractional Fourier Transform (FRT), which has one fractional-order. Under the linear transform, the Fourier transform (FT) captures the signal in the space domain and rotates it by 2 radians. It is orthogonally projected in the spatial frequency domain, while FRT is similar in that it rotates orthogonally in such a way that it gets mixed in the frequency space domain to perform operations. Hence, rotation angle is directly proportional to the FRT order. As a result, the FT is the ultimate fractional Fourier transform for its 1st order [15]. In optical encryption, FRT is used to encrypt two-dimensional data. As fractional orders are applied to the x- and y-axes, the system's performance, security, and robustness improve. It defends against blind decryption attacks. FRT should be unitary in nature, conserve power, and be completely reversible.

The Fresnel transform (FST)

It's a propagation of free space. Any FST is related to a FRT using quadratic step multiplication [16]. A particular category of LCT is the FST. This is a lensless technique that requires less hardware and is simpler to implement. Planes have three parts: input, transformation, and output. The encryption and decryption processes used the locations for RPM (random step masks) as keys. The cipher image was filmed in a photorefractive medium using holographic techniques. The "Random Phase Method" and the "Jigsaw Method" are always with the two optical encryption schemes focuses on the FST also given in the

approach. 3-phase keys in various Fresnel domains are used in the "Random Phase System." The input plane is attached to the first RPM (random phase mask), while the transform plane is attached to the second RPM. The cipher picture is generated when the device is illuminated perpendicularly with wavelength. The "Jigsaw Process," like the FRT, uses the Jigsaw transform (JT) in many Fresnel domains. Digital holographic methods necessitate encryption and decryption procedures of all frameworks.

Linear canonical transform (LCT)

The LCT transform is a multi-transform integral transform. It's a three-dimensional transform with four parameters and one restriction that's visualized in the time-frequency domain as the special linear group $SL(R)$. The FT, FRT, as well as FST are also all variants of both the linear canonical transform (LCT), and yet they all employ quadratic phase systems (QPS) to perform their calculations [17]. The image is encrypted using DRPE [29], and LCT is used. In this encryption scheme, the randomly generated propagators, the frequency, and all of the LCT specifications have been used as keys. Another word for it is Extended FRT. In the 2D LCT, the conditional integral transform includes three elements. It is possible to use the OFT, optical FRT, FST, even general LCT.

The Gyrtator transform (GT)

It falls under the category of linear canonical transforms (LCT). The GT is commonly used in optical as well as digital image recognition, holography, and model development [18]. The optical design for the GT has been recommended as three dimensions having circuit connecting across them. Every lens is made up of two identically driven convergent thin cylindrical lenses. The rotation of two thin cylindrical lenses regulates the transition angle. For a wide variety of angle parameters, this configuration will perform the GT. It belongs to the linear canonical transforms category (LCT). Using chaotic random phase masks, GT was used to encrypt the 2D file. The chaos feature manipulates the random process masks. The GT has been used as an optical image encryption scheme that employed a specific phase promising techniques. For color picture encryption, the DRPE scheme with the GT has been suggested. The affine transform and also the Arnold transform are two optical image processing approaches that are associated with GT (ART). In the sense of GT as a whole, The first random propagator $D1(x;y)$ multiplies the input image $I(x;y)$ before passing it into the first GT method of angle 1. The resulting image is then multiplied by the second random propagator $P2(x,y)$ and passed through the angle 2 GT method [29].

Ref	Year	Technique	Planes/class/phase	key	Security	Research Gaps from existing work	Proposed work improvements
[16]	2019	Symmetric cryptosystem	Symmetric cryptosystem	The intensity of the input image	High	Security achieved in this is high but the keys functionality is not good both the sides.	Use ECC for security.
[11]	2020	In the Fresnel transform domain, key image phase as well as chaotic random phase encoding	2 phase (image and chaotic)	Key phase mask	High	Authentication systems encode only one bit of encrypted form at a time, whereas cryptographic algorithms encrypt several bits at once (typically 64 bits in current ciphers). H	More than one bit will encrypt at a time.

[29]	2017	Gyrator transform	Every lens is made up of two identically driven convergent thin cylindrical lenses.	Using chaotic random phase masks, GT was used to encrypt the 2D file.	Much higher	Various companies use a variety of encryption schemes in the information systems field.	Proposed work can work on image as well as text.
[82]	2018	CKBA encryption method	Can produce a random sequence of good and suitable data encryption.	Image transitions and random map-based encryption	Good	Random sequence does not work sometimes.	The sender and receiver use separate keys and encryption/decryption data, implying that the key is shared. Asymmetric encryption is a term used to describe digital signature.
[12]	2011	Differential Evolution (DE) method	Keyed discrete Fourier transform (DFT) concept followed by DE operations for encryption purposes.	The secret key has been shared between both encryption	High	Secret key is same for both the sides.	Advanced version of the previous one.

Table 1: Comparison of DRPE based encryption techniques.

Factors	DRPE with AES		DRPE with 3DES		DRPE with ECC
Key Length	128,192	or	112,168		56 bits
	256 bits		bits		

Cipher Type	Symmetric		Symmetric	Symmetric
	block cipher		block cipher	block cipher
Block Size	128,192	or	64 bits	64 bits
	256 bits			
Developed	2000		1978	1977
Security	Considered		One	only
	secure		weak which	inadequate
			exit in DES	

Table 2: Comparative analysis over security algorithms.

S.no	Types of attacks	Parameter name	Description
1	Brute force attack	Key space	The brute force attack is described as guessing the correct key by evaluating the key value, which can be thwarted by using an algorithm with a sufficiently large key space.
2	Statistical attack	(i) Histogram analysis, (ii) Correlation coefficient analysis	(i) Details will be leaked if the values of pixels in the histogram are not standardized. As a result, uniform distribution is useful for fending off statistical attacks. (ii) The encrypted image must have a low overlap with neighboring pixels (horizontal, vertical, and diagonally).
3	Differential attack	(i) NPCR (ii) UACI	(i) Number of pixels change rate – $\frac{\sum_{s,t} D(s,t)}{M \times N} \times 100\%$ Where, M&N are width and height of image respectively, $D(s,t) = \begin{cases} 1, & c1(u, v) \neq c2(u, v) \\ 0, & otherwise \end{cases}$ Where C1 and C2 represent the ciphered image before and after pixel modification. (ii) Overall changing severity on a unified scale – $\frac{\sum_{u,v} C_1(u, v) - C_2(u, v) }{M \times N \times 255} \times 100\%$
4	Noise attack	(i) PSNR (ii) MSE	(i) PSNR(Peak signal to noise ratio) – It computes the quality of the recovered image $10 \times \log_{10} \frac{255 \times 255}{MSE} (db)$ (ii) Mean square error – It determines the MSE between the recovered and plain image.

			$\frac{1}{m, n} \sum_{p=1}^m \sum_{q=1}^n \ A_1(p, q) - A_2(p, q) \ ^2$ <p>Where A1 (p, q) is the original image and A2 (p, q) is the restored image, and m and n are the image width and height.</p>
5	Occlusion attack	PSNR(peak signal to noise ratio)	Any data may be lost during transmission, making decrypting the picture more difficult. It's used to see how the ability to retrieve plain images from ciphered images can be tested. PSNR is a metric that is used to assess occlusion efficiency.

Table 3. Parameters and description

No	Ref No.	Year	Technique	Key Space	Compressive Sensing	Speed
[1]	[31]	2016	Bitplane decomposition and chaotic maps	0.25×10^{64}	No	Low
[2]	[73]	2016	substitution cipher as well as synonymous.	10^{108}	No	Low
[3]	[74]	2016	Technique of dynamic random growth	$>10^{96}$	No	Moderate
[4]	[17]	2017	Hartley and Graytor transformation	$>2^{100}$	No	Low
[5]	[29]	2017	action on DNA sequence	8.39×10^{54}	No	Good
[6]	[49]	2017	disorderly structure with a cyclic change	$8^{256 \times 256}$	No	Low
[7]	[69]	2017	Map lattice with mixed linear-nonlinear coupling	$>10^{120}$ Moderate	No	Moderate
[8]	[71]	2017	Sensing that is compressed	3.4×10^{38}	Yes	Good
[9]	[72]	2017	Binary bitplane	4.916×10^{322}	No	Moderate
[10]	[75]	2017	Confusion-based swapping strategy	0.18×10^{60}	No	Good
[11]	[77]	2017	The map of Arnold	$>2^{100}$	No	Moderate
[12]	[81]	2017	Self-adaptive and disorderly spatiotemporal mechanism	10^{56}	No	Moderate
[13]	[85]	2018	Mapping logically	10^{112}	Yes	Moderate
[14]	[11]	2018	High-dimensional chaotic mechanism and spatial bit level permutation	1.03×10^{114}	No	Low
[15]	[22]	2018	Bit level permutation	10^{42}	No	Low
[16]	[23]	2019	Nonlinear optical multi-image encryption scheme canonical transform	2.5×10^{57} , which is large	No	Low
[17]	[24]	2019	Nonlinear chaotic system and linear canonical transformation	Pixel scrambling	Yes	Low

[18]	[25]	2021	Optical image encryption based on quantum walks	10128	No	Good
[19]	[26]	2021	Exploiting optical chaos	10114	Yes	Moderate
[20]	[27]	2021	Hadamard single-pixel imaging and Arnold transformation	coefficient matrix increases	No	Low
[21]	[28]	2021	Secure Optocrypto system for 2D logistic based fractional fourier	2D-FrFT angles and fractional orders	No	Moderate
[22]	[29]	2021	A fast and secure public-key image encryption scheme based on Mordell elliptic curves	public-key image encryption	No	Good

Table 4: Comparison of techniques based upon parameters

Techniques	Advantages	Disadvantages
Runlength Encoding	Simple and not require CPU power,	Useful for files with such a lot of effective combination.
Fractal Encoding	Good Encoding frame	sluggish encoding.
LZW Encoding	A complex codeword table is created	It takes up more data storage,
Arithmetic encoding	fractional values	complicated tasks
Vector Quantization	simple converter with no parameter approximation.	correct code at a very slow pace.
Huffman Encoding	data compression is both easy and effective	Good estimation is necessary for good results.
Double Random Phase Encoding (DRPE)	two random process masks. Loading time is short.	Speckle noise due to the random phase mask
Off-axis holography system	Support 3D object watermarking	Reference wave required
Phase shifting holography system	Support 3D object watermarking;	Reference wave required; Multiple host images required
Cascaded phase only mask architecture	Non-destructive to host image	Hard to implement in real optical experiment
Joint Transform Correlator (JTC)	Easy to implement optically	Not applicable for watermarking 3D object
Ghost imaging system	Simplest image detector	Long image acquisition time; Noise in reconstructed image

Ptychography	Support 3D object watermarking; resistant; Easy to implement optically	Noise	Recording of multiple diffraction patterns required

Table 5: Image compression and scrambling algorithms.

3. Problems Discussion

- (1) Some sensor networks, along with DRPE and interleaved stage only mask systems, are complex to realize in optical applications probably a combination of processes needed underneath coherent light illumination. This problem can be fixed by combining these optical devices with indecipherable operations like authentication scheme [44,45], in which a true deciphered result is generated by an approximate combining (as well as a very precise integration) of integrated circuits.
- (2) By analyzing main reference brightness patterns [46] and iterative reconstruction algorithms [47], different imaging speed in a ghost imaging system can be accelerated for watermarking. Information security and imaging speed must both be guaranteed at the same time.
- (3) For a ptychography device, the amount of waste it collects is immense (multiple diffraction patterns). A compressed method must be developed to reduce data size while enhancing the stability of the retrieved wavelet domain [48].

The subsequent section contains various objectives required to accomplish the proposed technique: To study and analyze the performance of optical image encryption algorithms.

- To design and implement novel lensless phase-based image encryption techniques.
- To utilize efficient transform domain approaches to enhance the proposed techniques further.
- To compare and validate the proposed technique with the existing optical image encryption techniques using some well-known quality metrics.

4. Conclusion

This paper discusses the latest optical picture encryption methods in depth. This paper based on the DRPE methodology and the different transforms that can be used in DRPE to enhance image protection. The procedure is an addition of a well-known DRPE framework that includes an additional random phase key. The efficiency of the proposed scheme is assessed, and it is observed that it is comparable to DRPE in terms of PSNR and MSE metrics, but it provides better security.

The benefits and drawbacks of fractional transformations, Fresnel transforms, Hartley transforms, and Gyrator transforms were explored. Optical picture encryption methods have been addressed in terms of their challenges and potential study directions. Optical image encryption is still an underdeveloped area, according to a study of emerging optical image encryption techniques. For upcoming projects, an alternative to building a robust and reliable technique by combining the optical encryption method with different encryption techniques.

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